

## Jet Aircraft Electric Field due to its Exhaust Gases

Research Article

Theodore I. Lekas\*

Department of Aerodynamics and Flight Mechanics, Hellenic Air Force Academy, Dekelia AFB, TGA 1010, Dekelia, Attika, Greece.

### Abstract

During flight, an aircraft acquires an electrostatic charge distribution on its skin due to various reasons, among which is the electrostatic polarity of the exhaust gases. Due to this electrostatic charge distribution, the aircraft, induces an electrostatic field at any point of its surrounding area. In this paper, a fast quantitative approach is proposed in order to compute the strength of this electrostatic field so as to determine if the break down electric field threshold for air ionization can be exceeded. If so, a stepped leader from an electrified cloud could be directed towards the aircraft, resulting in a lightning strike. This approach is based on the common mathematical background of potential flow and electrostatics. It was found that the strength of the electrostatic field induced by the aircraft is much less than the break down electric field threshold, therefore a lightning strike on the aircraft is unlikely to occur.

**Keywords:** Aircraft; Exhaust; Soot Particles; Electrostatic Charging; Electric Field; Panel.

**List of Symbols:**  $U$  = electrostatic potential (V);  $x, y, z$  = coordinates of a target point in a panel frame of reference (m);  $x_k, y_k, z_k$  = coordinates of panel corner point  $k$  in a panel frame of reference (m);  $\vec{n}, \vec{t}, \vec{l}$  = right orthogonal frame of reference at the centroid  $G$  of each panel;  $\vec{n}$  = panel normal unit vector pointing outwards;  $\vec{t}, \vec{l}$  = unit vectors tangent to the panel and such that  $\vec{n}, \vec{t}, \vec{l}$  be right orthogonal;  $\vec{E}_R$  = resultant electric field vector at a given point (V/m);  $q$  = electrostatic charge strength distribution at the surface of each panel (Coulomb) per  $m^2$ .

### Introduction

In flight, the skin of an aircraft is electrostatically charged, mainly due to a thunder cloud proximity, friction with the surrounding airflow, impacts of atmospheric crystals (p-static charging) and exhaust gas polarity. Thus, the aircraft induces an electrostatic field at any point of its surrounding area. In case of flight in a region where an ambient electrostatic field exists, as for instance in the vicinity of a thunder cloud, due to the resultant electrostatic charge distribution on the aircraft skin, a stepped leader might be attracted [1-3]. The electrostatic charging of the aircraft due to the exhaust gas polarity can also create a radio frequency interference according to [4].

Engine exhaust gases contain a large amount of charged particles, called soot particles. Soot particles can be generated during the combustion or by flow disturbances in the gas path, for instance blade rubbing or abnormal combustion [5, 6]. Exhaust gases are slightly more ionized than the surrounding air, so it is unlikely that

they can attract a step leader or create a lightning flash (in contrast to rocket exhaust plumes). By discharging electrostatic charges through its exhaust gases, a jet aircraft acquires an electrostatic charge distribution on its skin, of opposite sign.

The electric field induced by this electrostatic charging of the skin creates radio frequency interference which depends on aircraft configuration and engine type. This disturbance increases the ambient noise level of the equipment, making reception difficult [4]. On the other hand, unlike the case of p-static charging procedure, no corona discharge is noticed in fair weather conditions flight [7], which might indicate that the effects of the electrostatic charging of the aircraft due to engine exhaust gases polarity can be neglected. This is supported by the fact that entry points are, so far, never reported on the engine exhaust, except if the exhaust is located at the rear extremity of the aircraft [7].

In order to have a quantitative insight of the problem, in this paper an approach for computing the electrostatic charges distribu-

#### \*Corresponding Author:

Theodore I. Lekas,  
Department of Aerodynamics and Flight Mechanics, Hellenic Air Force Academy, Dekelia AFB, TGA 1010, Dekelia, Attika, Greece.  
Email: tlekas@hotmail.com

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tion acquired on the skin of an aircraft of arbitrary geometry due to the exhaust gases electrostatic polarity, is presented. It is based on measured electrostatic potential acquired by an aircraft due to jet engines exhaust gases [8]. This approach uses singularities and is based on the fact that electrostatics and potential flow theory have the same mathematical background.

The resultant electric field induced by the electrostatic charges acquired by the aircraft at points of the surrounding area nearby extremities like wing, horizontal stabilizer and vertical fin tips, as well as nearby the nose and the rear cone extremity will then be calculated. The above locations are chosen because of their relatively small curvature radius. These values will be compared to the corresponding breaking down electric field value of air, which equals to 300.000 V/m.

### Presentation of the Approach

The external surface of an aircraft of arbitrary geometry is described by a number of points, which are combined by three or four so as to form plane panels. The coordinates of these points are expressed in a global frame. The origin O of this frame is located at the nose of the aircraft, the  $\vec{X}$  axis is parallel to the longitudinal axis of the aircraft and directed towards the tail, the  $\vec{Y}$  axis is parallel to the span and directed towards the right wing tip (pilot's point of view) and the  $\vec{Z}$  axis is such that the frame  $\vec{OX}\vec{Y}\vec{Z}$  is a right orthogonal one.

The dimensions of each panel are sufficiently small, while the number of panels is sufficiently high so as to avoid gaps and to describe as closely as possible the aircraft's geometry. It must be pointed out that there is a threshold number of panels, depending on the geometry of the aircraft, above which numerical problems usually occur. Each panel carries a homogeneous electrostatic charge distribution  $q$ , which has to be calculated. The electrostatic charge of the metallic parts of the aircraft skin induces an electric field at any point of the surrounding area.

According to [8], the electrostatic potential  $U$  acquired by an aircraft due to its exhaust gases polarity can reach a value of -105 Volts. Due to the common mathematical background of electrostatics and potential flow theory, the aerodynamic potential of a source/sink distribution on a panel [9] can also be used for electrostatic calculation purposes. All panels of the aircraft skin are at the same electrostatic potential  $U$ . The electrostatic potential  $U$  of each panel is expressed in a panel right orthogonal frame (local frame  $G\vec{n}, \vec{i}, \vec{l}$   $G$  being the centroid of the panel). Since all corner coordinates are expressed in the global frame (or initial frame), a transfer from the global to the local frame and vice versa, is needed.

For electrostatic purposes, the flow potential equation is adequately modified. The electrostatic potential  $U$  induced by each panel at a given point located at a position  $x,y,z$  in panel coordinates is given by equation (1):

$$U = \frac{q}{4\pi\epsilon_0} \sum_{K=1}^N \left\{ \left( \frac{(x-x_K)(y_{K+1}-y_K) - (y-y_K)(x_{K+1}-x_K)}{d_{KK+1}} \right) \ln \left( \frac{r_K + r_{K+1} + d_{KK+1}}{r_K + r_{K+1} - d_{KK+1}} \right) + \left| z \left( \tan^{-1} \left( \frac{m_{KK+1} e_K h_K}{z r_K} \right) - \tan^{-1} \left( \frac{m_{KK+1} e_{K+1} h_{K+1}}{z r_{K+1}} \right) \right) \right| \right\}$$

$$d_{K K+1} = \sqrt{(x_{K+1} - x_K)^2 + (y_{K+1} - y_K)^2}$$

$$m_{K K+1} = \frac{y_{K+1} - y_K}{x_{K+1} - x_K}$$

$$e_K = (x - x_K)^2 + z^2$$

$$h_K = (x - x_K)(y - y_K)$$

$$r_k = \sqrt{(x - x_k)^2 + (y - y_k)^2 + z^2}$$

where  $q$  is the electrostatic charge distribution (Coulomb/m<sup>2</sup>) of the panel,  $\epsilon_0$  is the electrical permittivity of the air (8,85 10<sup>-12</sup> F/m),  $x_k, y_k, z_k$  are the coordinates of the panel corners and  $x,y,z$  the coordinates of the target point (m), all expressed in a panel frame.  $N = 3$  or  $4$  for a triangular or a four corner panel respectively.

The electrostatic potential induced by all panels  $j$  to the centroid of panel  $i$  (the target point in this case) is given by equation 2:

$$\sum_{j=1}^M v_{ij} q_j = U \quad \text{---- (2)}$$

where  $v_{ij}$  is the potential induced on panel  $i$  by a panel  $j$  carrying an electrostatic charge distribution equal to 1.  $q_j$  is the electrostatic charge distribution carried by panel  $j$ , which has to be calculated.  $M$  is the total number of panels approximating the external surface of the aircraft.

By applying equation (2) at the centroids of all  $M$  panels describing the surface of the aircraft, an  $M$  by  $M$  system of linear algebraic equations is obtained. The right hand side of the system is equal to the potential of the skin of the aircraft, which is constant and has the same value at all panels since the skin is an equipotential surface. So, the value of the electrostatic potential acquired by the aircraft skin due its exhaust gases polarity is the boundary condition of the computation.

The resultant electric field  $\vec{E}_R$  induced by the electrostatic charge of each panel at any given point around the aircraft is based on the fact that:

$$\vec{E}_R = -\overline{grad} \left( \sum_{i=1}^M U_i \right) \quad \text{---- (3)}$$

where  $U_i$  is the contribution of the  $i^{\text{th}}$  panel on the resultant electric field. The components of  $\vec{E}$  induced by all panels at a given point, in panel coordinates, are  $E_x, E_y$  and  $E_z$ .

In order to obtain the exact forms of  $E_x, E_y$  and  $E_z$  a rather lengthy process of derivation is required. Since these forms are rather lengthy and complicated, for space saving reasons they are not presented here. It must be pointed out that, in order to obtain the resultant field due to all panels, the above components are to be transferred in the  $\vec{OX}\vec{Y}\vec{Z}$  frame of reference.

## Results and Discussion

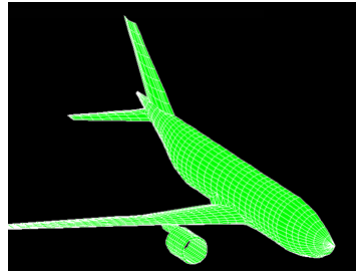
A numerical generic airliner geometry of 50 m length and 60 m wingspan is created and shown in figure 1. Due to the symmetry of the aircraft about a plane perpendicular to the span, only its half is presented in Figure 1, but in the computation of the electrostatic charges the entire aircraft geometry is taken into account through symmetry projections. An in-house numerical code was used for the electric field calculation. The M by M linear algebraic equation system is solved based on a singular value decomposition numerical method [10]. This approach can be applied to any

aircraft geometry, propulsion system type and electrostatic potential value.

Table 1 shows the strength of the induced electric field at the extremities of the aircraft for initial skin electrostatic potential values of -104, -105 and -106 V respectively. In all cases, the points of interest are at a distance of 0.5 m from the aircraft.

From table 1, it can be seen that the induced electric field strength is always less than 300.000 kV/m, so no ionization of the air occurs. Whether a radio frequency interference occurs or not, de-

**Figure 1. Generic airliner geometry.**



**Table 1. Strength of the Induced electric field in kV/m at the extremities of the aircraft for exhaust gases electrostatic potential values equal to  $-10^4$ ,  $-10^5$  and  $-10^6$ .**

| EX. GAS POTENTIAL (V) | $-10^4$ | $-10^5$ | $-10^6$ |
|-----------------------|---------|---------|---------|
| NOSE                  | 1,477   | 14,775  | 147,751 |
| REAR CONE             | 1,106   | 11,054  | 110,540 |
| WING TIP              | 1,720   | 17,207  | 172,077 |
| HOR. STAB. TIP        | 0,751   | 7,513   | 75,134  |
| VERT. STAB. TIP       | 0,339   | 3,398   | 33,982  |

depends on the technical specifications of the corresponding equipment. But, it seems unlikely that a stepped leader can be attracted.

## Conclusion

In this paper, a quantitative approach was presented to compute the strength induced due to the exhaust gases polarity of a jet aircraft. It was found that the strength of the induced electric field close to the wing, horizontal stabilizer and fin tips, as well as close to the nose and the rear cone is less than the corresponding value of the break down electric field of air. Consequently it is unlikely a stepped leader can be directed towards the aircraft due to the exhaust gas polarity. It also appears that there might no influence on the navigation and communication systems of the aircraft, of course according to their specifications.

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