Evaluation of Relative Permeability Tests One-Step with Bump Flow and Multi-Step

Santos ICABA1*, Eler FM2, Nunes DSS2, Cordeiro Júnior CR2 and Couto P1

1Federal University of Rio de Janeiro, Civil Engineering Program, Brazil
2COPPETEC, Rio de Janeiro, Brazil

*Corresponding author: Iselly Christinne ABA Santos, Federal University of Rio de Janeiro, Civil Engineering Program, Rio de Janeiro, RJ, Brazil, Tel: +5588988836855; Email: isabellysantos@coc.ufrj.br

Abstract

The relative permeability curves obtained in the laboratory are used in reservoir simulators to predict production and decide the best strategies for an oil field. Therefore, researchers are studying several procedures to obtain relative permeability curves, among them the multiple flow rates injection methods. Thus, this work proposes to develop an experimental procedure with multiple increasing flows (multi-step). To make this feasible, simulations were initially carried out at CYDAR, aiming to establish the flow rates and necessary the time to system stabilization, within the limits of the equipment. After that, the tests were carried out and the results obtained were the minimum time of 5 hours to stabilize the oil production and the differential pressure at each flow rate. The accounting and minimization of the capillary end effect in these tests were also evaluated. And the capillary pressure constraints contributed to minimize the number of possible solutions of the optimization problem improving the uniqueness of solution.

Keywords: Relative Permeability; Multiple Flows Rates; Cydar; Capillary End Effect

Introduction

Relative permeability is one of the most important data for reservoir engineering. The relative permeability curves obtained in the laboratory are used in reservoir simulators to predict oil production and decide the best strategies when exploring an oil field [1].

The tests to obtain these curves, in a water-oil system, are performed on rock samples from the reservoir or on representative outcrops. These are often subjected to displacement tests in an unsteady-state regime, in which an attempt is made to repeat the fluid displacement processes that take place in the oil reservoirs during secondary recovery activities. In the test, capillary and viscous forces act in the rock sample, as well as in the petroleum reservoirs [1,2].

Usually, this experiment is conducted by injecting water at a single constant flow rate. The experimental data obtained (differential pressure and produced volume of oil) is treated by analytical techniques, such as that of JBN [3], or by history matching, to obtain the parameterized relative permeability curves ($K_r$). However, these tests have limitations and conditions that are intrinsic to the laboratory, differently from what occurs in real reservoir flows, such as the capillary end effect. This happens due to a discontinuity in capillary pressure at the end sample outlet, causing an erroneous residual oil saturation [4,5].

Besides, many mathematical methods used to infer the $K_r$, as the JBN, do not consider the capillary forces, and
the method of history matching does not guarantee the uniqueness of solution if used in experiments with only one injection flow rate. This can generate bias in the relative permeability obtained in the laboratory [6].

In the exposed context, the present work proposes to develop an experimental procedure of multiple flow rates, to obtain the relative permeability curves, based on the theoretical methodology proposed by Lenormand & Lenormand [7].

The greatest advantage of this method is the accounting of the oil that was retained in the sample due to the capillary end effect. Furthermore, there is the possibility of determining both the capillary pressure ($P_c$) and relative permeability ($K_r$) in a single experiment and also to add a capillary pressure constraint to improve the uniqueness of the history match process.

Relative Permeability Experiments

During the drilling process of reservoirs, rock cores are extracted and undergo several laboratory tests to determine properties of relevance for oil extraction, such as porosity, permeability, and capillary pressure. Laboratory experiments must be carried out at reservoir conditions so that the results obtained are representative of the field.

In Figure 1, one of the most used core flooding experiments to determine the ($K_r$) is presented, it is called the unsteady state relative permeability. The Unsteady-State (USS) method consists of displacing the fluid that saturates the porous medium by injecting another fluid at constant flow or constant pressure [8].

![Figure 1: Scheme of the relative permeability test in transient regime [9].](image)

For a water-oil system, an oil-saturated core with immobile water ($S_{wi}$) is first accommodated in the holder. This condition is representative of the initial state of the reservoir before the injection of fluids for its exploitation. Then, it is performed a water injection in the inlet face, while oil is produced at the outlet face. During the test, the produced oil volume and the differential pressure across the core are recorded.

The most used laboratory procedures in the water-oil relative permeability tests consists of the injection of water at a single flow rate, obtaining the residual oil saturation ($S_{or}$). The $S_{or}$ can be greatly affected by the capillary end effect [10]. Thus, to minimize laboratory artifacts, a sudden increase in flow rate (bump flow) is performed at the end of the test. There is often an additional production of oil-related to the increase in differential pressure caused by the bump flow [1]. For identification purposes, the residual oil saturation ($S_{or}$) will be called remnant $S_{or}$ ($S_{or}^{rem}$) when it is obtained in a test with only one injection rate and bump $S_{or}$ ($S_{or}^{bump}$) when there is an increase in flow rate (bump flow).

Converting Laboratory Data to Relative Permeability

The relative permeability curves are inferred from the differential pressure and oil production data collected in these tests. The solution techniques normally applied are analytical solutions, such as JBN [3,11], based on the Buckley-Leverett model for the displacement of immiscible fluids.

This method assumes simplifications such as one-dimensional flow, negligible capillary pressure, and homogeneous porous medium. These simplifications hardly represent the reality of the displacement tests performed in the laboratory [9,12].

Another technique very used is the history matching [13], which is a non-linear regression problem. The procedures of this nature use parameterized $K_r$ curves in a numerical flow simulator and an optimization process finds the parameters that best represent the experimental data. In this type of technique, the flow model can be simplified or not.

The advantage of this method is the possibility of including all effects that may be relevant in the actual displacement process, such as capillary pressure, medium heterogeneity, fluid compressibility, or gravity [9,14]. However, many software that uses the non-linear regression method do not include these effects in the theoretical model, analyzing the data up to ($S_{or}^{rem}$), as in JBN [1].

Multistep Procedure

The multiple flow rates test should be considered over the traditional one (single flow rate plus bump flow), even if that lasts longer than this. Because the experiments in several increasing flow rates provide $K_r$ and $P_c$ curves simultaneously [10].
In the technique proposed by Lenormand & Lenormand [7], the test is started by injecting water into the sample at constant flow until the oil production and differential pressure stabilize. Then, the flow rate is increased until the new stabilization is achieved. This process is repeated using 5 to 10 steps of injection rates. With each rate, additional oil is produced and the average water saturation increases. With these data, it is possible to account for the capillary end effect and the amount of oil that was retained due to this phenomenon. At the end of the test, \( S_{w, r} \) is expected to be closer to the real \( S_{w} \) [4].

### Materials and Methods

#### Materials

The rock samples used were homogeneous outcrops of the Berea Buff formation, obtained from Kocurek Industries. To minimize the influence of the type of sample in the tests, the same 20 cm core was split into smaller cores, approximately 5 cm each. The basic properties of these samples are shown in Table 1.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Length D (cm)</th>
<th>Diameter D (cm)</th>
<th>Absolute Permeability ( K_{abs} ) (mD)</th>
<th>Porosity ( \phi ) (frac.)</th>
<th>Porous Volume ( V_p ) (cm³)</th>
<th>Irreducible Water Saturation ( S_{w, i} )</th>
<th>( K_r ) test</th>
<th>Alteration of rock wettability</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sample 1</td>
<td>4.78</td>
<td>3.82</td>
<td>597</td>
<td>0.225</td>
<td>11.99</td>
<td>0.202</td>
<td>Bump flow</td>
<td>-</td>
</tr>
<tr>
<td>Sample 2</td>
<td>4.84</td>
<td>3.82</td>
<td>602</td>
<td>0.227</td>
<td>12.24</td>
<td>0.187</td>
<td>Multi-step</td>
<td>-</td>
</tr>
<tr>
<td>Sample 3</td>
<td>4.9</td>
<td>3.82</td>
<td>601</td>
<td>0.228</td>
<td>12.5</td>
<td>0.208</td>
<td>Multi-step</td>
<td>-</td>
</tr>
<tr>
<td>Sample 3*</td>
<td>4.89</td>
<td>3.81</td>
<td>515</td>
<td>0.227</td>
<td>12.41</td>
<td>0.122</td>
<td>Multi-step</td>
<td>Saturation of rock with SAN**</td>
</tr>
<tr>
<td>Sample 4</td>
<td>4.61</td>
<td>3.82</td>
<td>597</td>
<td>0.228</td>
<td>11.79</td>
<td>0.169</td>
<td>Multi-step</td>
<td>Sample aging with OMN***</td>
</tr>
</tbody>
</table>

Table 1: Properties of the sample and fluids used in the USS experiment multiple flows. *Sample subjected to a new \( K_r \) test after cleaning; ** SAN - naphthenic aqueous solution; *** Naphthenic Mineral Oil

The fluid used as the oil phase was the EMCA PLUS 70 and Naphthenic Mineral Oil, as the aqueous phase a brine with a composition equivalent to that of the Brazilian Pre-Salt fields was used. The physico-chemical properties of fluids under test conditions are shown in Table 2.

<table>
<thead>
<tr>
<th>Fluid</th>
<th>Density ( \rho ) (g/cm³)</th>
<th>Viscosity ( \mu ) (cP)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mineral Oil (OM)</td>
<td>0.856</td>
<td>23</td>
</tr>
<tr>
<td>Naphthenic Mineral Oil (OMN)</td>
<td>0.848</td>
<td>23.5</td>
</tr>
<tr>
<td>Brine</td>
<td>1.142</td>
<td>1.48</td>
</tr>
</tbody>
</table>

Table 2: Physico-chemical properties of fluids at 21°C and ambient pressure.

#### Methods

Two types of coreflooding experiments were carried out: without changing the wettability of the rocks and with changing the wettability of the rocks (Table 1).

In general, in both tests, the USS water-oil relative permeability experiment at laboratory scale (Figure 2) followed the sequence of procedures proposed by Viegas [12]:

1. Cleaning the sample in Soxhlet apparatus, using methanol and methylbenzene (toluene).
2. The routine core analysis to obtain the basic properties of the samples, such as absolute permeability and effective porosity.
3. Total saturation of the samples with the brine of composition equivalent to the water of formation of the fields of the Brazilian Pre-Salt.
4. Centrifugation of samples in an oil environment to obtain irreducible water saturation \( S_{w, i} \).
5. Accommodation of the core sample on a hydrostatic confinement cell, using 1,000 psi of confining pressure.
6. Measurement of effective oil permeability at irreducible water saturation \( K_{re} @ S_{w, i} \).
7. Displacement of mineral oil by injection of brine to the state of residual oil saturation \( S_{o, r} \), with monitoring of
oil production \( (N_p) \) and differential pressure \( (\Delta P) \):

1. With a constant flow of 1 cm³/min plus a bump flow of 4.0 cm³/min in the traditional test.
2. With five flow levels in the multistep test: 1.0, 2.0, 4.0, 8.0 and 10 cm³/min.
3. Measurement of effective water permeability in \( S_{we} \).

The tests on rock samples with alteration of wettability distinguished from the others due to the addition of the following procedures:

1. Sample 3*: Alteration of wettability with saturation of naphthenic aqueous solution (SAN): this procedure involved saturating the rock sample with the naphthenic aqueous solution for 24 h at 2,000 psi. The sample was removed from the saturation system and placed in the oven for the drying step. Subsequently, the sample was subjected to new saturation with balanced brine of a composition equivalent to that of the Brazilian pre-salt for 24 h at 2,000 psi. Subsequently, the sample was sent to determine the \( S_{wi} \) in the centrifuge, and was subsequently confined to the coreholder without carrying out the aging stage.

2. Sample 4*: Alteration of wettability with naphthenic mineral oil (OMN): this procedure involved the injection of a naphthenic organic solution diluted in mineral oil in the rock sample at \( S_{wi} \). About 8 injections with OMN were performed on alternate days, with a flow rate of 0.5 cm³/min and a flow rate of 1.0 cm³/min until stabilization \( K_r \) in the 88% range (aging stage).

The experimental data was used to estimate the relative permeability and capillary pressure by history matching. The software CYDAR® was used to estimate the parameters of the used models: LET model [15] for relative permeability and \( \log(S^B) \) model [16] for capillary pressure.

### Results and Discussion

#### Analysis of Water-Oil Relative Permeability Tests Considering Capillary Pressure

Figure 3 shows the experimental data from Sample 1, in which water was injected at a flow rate of 1.0 cm³/min for 23 hours. At the end of this first injection, 6.25 cm³ of oil was produced. The bump flow, with a flow rate of 4 cm³/min, was carried out afterward and the \( \Delta P \) stabilized after 1 hour and there was no additional oil production. Returning to a flow rate of 1.0 cm³/min, the \( \Delta P \) stabilized after 30 min. Thus, the traditional test with the bump flow was completed in 24.5h.

![Figure 3: Experimental data obtained in the traditional water-oil relative permeability test with bump flow (points) and data obtained by the history-matching process (solid line) to obtain Kr and Pc curves. a) Differential pressure versus time. b) Volume of produced oil versus time.](image)

Figure 4a shows the capillary pressure curve estimated for the imbibition test. As shown by Abdallah et al. [17] the sample showed results from a water-wet sample, where the capillary pressure remains positive during most of the saturation range, as shown in Figure 4a. Thus, water saturation preferably increases first in the smallest pores, due to wetting forces, so the displacement occurs from the smallest to the largest pores, and the water increasingly occupies the throat of pores that were previously filled with oil, as shown in Figure 4b, which presents the relative permeability.

According to Masalmeh [18], water-wet samples have very well-defined residual oil saturation and are insensitive to the flow rate, that is, \( S_{or} \) is not affected by the increased flow rate. Analyzing Figures 3 and 4, it is possible to infer that the sample is water-wet, so there was no additional production associated with bump flow, so \( S_{or} \) was equal to \( S_{or}^{bump} \) (Figure 3b).
Figure 4: Curves estimated in CYDAR, using history matching. a) Capillary pressure curve as a function of water saturation. b) Relative permeability curves as a function of water saturation.

In Figure 5, the data of Sample 2 and Sample 3 are presented, which were submitted to the multistep process. In Figure 5a it is identified that in the first test flow the Sample 1, 7.80 cm³ of oil was produced, and at the end of the 30 hours test, 7.93 cm³ had been produced, that is, even increasing the flow 10 times, there was a gain of only 1.7% in the volume of fluid produced about a flow of 1.0 cm³/min. While in Sample 3, shown in Figure 5b, the first flow of 1.0 cm³/min produced 7.25 cm³ during the initial 5 hours, ending the test with 7.50 cm³ of displaced oil. Thus, the 10-fold increase in flow provided a small gain of 3.4% of the oil produced about the initial flow.

Figure 5: Experimental data obtained in the multi-step water-oil relative permeability test (points) and data obtained by the history-matching process (solid line) to obtain $K_r$ and $P_c$ curves. a) Sample 2. b) Sample 3.

The capillary pressure and relative permeability curves, presented in Figure 6 and Figure 7, fitted the experimental data with precision, as shown in Figure 5. In Figure 6, the $P_c$ curves are positive in most of the water saturation range, representing water-wet samples. Also, adapting the calculation of the USBM index for the imbibition test, which measures the wettability using the areas under the positive and negative capillary pressure curves, this water wettability is confirmed, since the results are values greater than 1 [17].
Besides, interpreting the $K_r$ curves in Figure 7, it is noticed that water begins to enter the smaller pores first, and as the water saturation increases, the pores are filled sequentially from the smallest to the largest, as well as a preferably wettable sample. water, as explained by Crotti [19].

The average water saturation $\langle S_w \rangle$ versus capillary pressure data presented in Figure 6 was obtained by the procedure proposed by Lenormand & Lenormand [7]. This procedure assumes that at the end of each flow rate, as oil production stops, the oil phase is not moving, therefore the differential pressure for this phase equals to zero ($P_o$). This implies that the differential pressure measured across the sample is the water phase differential pressure ($P_w$) (Figure 8 and Equation 1). In Equations 2 and 3 it is demonstrated how these calculations are performed.
\[ P_W = \Delta P \quad (1) \]
\[ P_C = P_O - P_W = 0 - \Delta P \quad (2) \]
\[ P_C = -\Delta P \quad (3) \]

This data points of \( P_C \) vs \( S_w \) were used in CYDAR as an experimental constraint to the estimated capillary pressure, improving the solution uniqueness problem, faced in history matching process. Comparing the experimental and estimated data it is possible to conclude that the constraint was satisfied with great precision.

**Tests with Change in Wettability Using Naphthenic Mineral Oil in Aging**

Sample 4 was submitted to the aging process, aiming to change its wettability, since sample 2 and 3 taken from the same core were wettable to water.

Figure 9 shows the experimental data obtained in sample 4, submitted to the multiple flow test with aging using OMN. The test started with the injection of water at a flow rate of 1 cm³/min, stabilizing \( N_p \) and \( DP \) in 5 h after starting the pump. The volume obtained, in the inverted separator, in this first flow was 6.85 cm³. At the end of the test, 7.75 cm³ of the produced fluid was displaced. Thus, the increase of 10 times in the flow, provided a gain of approximately 13% of oil produced in relation to the initial flow, that is, there was a significant change in the \( S_{w}^{n} \). During the test stabilization at 1 cm³/min, the sample’s \( S_{w}^{n} \) was 0.25, while at the end of the test, at 10 cm³/min, there was a decrease in oil saturation to 0.17.

Additionally in Figure 9, it is analyzed that the estimated water-oil relative permeability and capillary pressure curves, shown below in Figure 10a and Figure 10b, respectively, adjusted the data well.

Interpreting the \( K_r \) curves in Figure 10a, the crossing of the curves occurs at \( S_w < 0.5 \), common for oil-wettable samples, that is, water begins to enter the larger capillary tubes, and as the water saturation increases, the tubes are filled sequentially from largest to smallest [19]. However, analyzing the \( P_C \) curve, Figure 10b, the capillary pressure remains positive during most of the saturation range, crossing the axis at approximately 0.7 saturation, and the USBM index was 0.658. Thus, it was not possible to conclude whether the sample is strongly wettable to water or oil, being considered with mixed wettability. Another point to be noted in Figure 10b, was how much the experimental points of \( S_w \), calculated from Equation 3, approached the water saturation on the face, estimated on the \( P_C \) curve.

**Using naphthenic aqueous solution in saturation**

Sample 3 was subjected to a new test of relative permeability water-oil of multiple flows, after cleaning, being named sample 3*. In this test the sample was saturated 100% in naphthenic aqueous solution, aiming to change its
wettability.

The experimental data obtained in sample 3* are shown in Figure 11. The volume obtained, in the stabilization of the first flow, 1 cm³/min, was 6.30 cm³. At the end of the test, 6.85 cm³ of the produced fluid was displaced. Thus, the 10-fold increase in flow, provided an increase of 6.6% of oil produced in relation to the initial flow.

Additionally in Figure 11, it is analyzed that the estimated water-oil relative permeability and capillary pressure curves, shown below in Figure 12a and Figure 12b, respectively, adjusted the data well.

The water-oil relative permeability curves, shown in Figure 12a, intersect approximately at the 0.56 S_w, showing a tendency of the sample to remain water-wettable. The capillary pressure curve has a USBM index of 0.44, the crossing of the curve occurs approximately at 0.53 saturation (Figure 12b). Thus, it is not possible to conclude whether the sample is strongly wettable to water or oil, being considered with mixed wettability.

Analysis of Saturation Profiles

Saturation profiles at the end of each flow rate were also obtained by the history-matching process (Figure 13). It is possible to notice that the increase in flow rates causes an increase in the average water saturation and, consequently, an increase in oil production, as it was shown.
In addition, the saturation profiles become more uniform over the length of the sample as the flow increases, converging on the sample’s outlet face. In Figure 13, it is possible to observe that the oil is stuck at the end of the core sample, due to the edge effect [20].

**Conclusions**

From the relative permeability experiments carried out, in three sandstone samples of the same petrophysical properties, but comparing different methodologies—Sample 1 with conventional test; Samples 2, 3 and 4 with multi-step - it is possible to conclude that:

1. In high permeability water-wet and mixed-wet samples the stabilization of the differential pressure and produced volume is achieved in 5 hours, at each imposed flow rate.
2. In general, the samples submitted to the multi-step test further minimize the capillary end-effect than the traditional bump flow test, mainly making the saturation profile more uniform over the length of the sample, so in the multiple flow tests it is possible to account for the edge effect.
3. The relative permeability and capillary pressure curves obtained simultaneously in the same experiment reduce the problem of non-uniqueness of the solution, associated with the non-linear regression calculations applied in the historical adjustment.

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