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**HIERARCHY OF PLANE CONTOURS THROUGH TREES STRUCTURES
WITH THE STRUCTURE LIST**

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ABSTRACT

Paper presents an original method proposed by Dora Florea for hierarchy of the plane contours in trees structures, express through a structure liste, starting from the knowledge the position relation between two contours.

KEYWORDS: Plane contour, tree structure, position relation, hierarchy

INTRODUCTION

A matricial representation of the trees was proposed by T.Rus [1] and so it know the representation of a contours tree structure by structure list .

Requiring position relation aspect between two by two contours , belong of a contours collection defined as atomic objects expresses with the matricial representation , in this paper Dora Florea propose an original method to obtain a composition structure of the tree or forest composed from atomic objects which are contours express with add the structure list.

THEORETICAL CONSIDERATION

Beeing gived the contours collection $M_c = \{C_i | i = 1..n\}$ closed and coplain, contours may be considered as the atomic objects of a complex structure of which composition may be describe by a tree or forest atomic objects. In Fig.1 it evidences an composition tree of a forest type composed from 3 disjunct trees and which it may be graphic presents as in Fig.2.

Contours structure from Fig.1 may be represents by a structure list:

$$L=(C_5(C_3(C_1),C_4(C_2),C_{12}),C_6(C_7,(C_8,C_9)),C_{11}(C_{10}))) \tag{1}$$

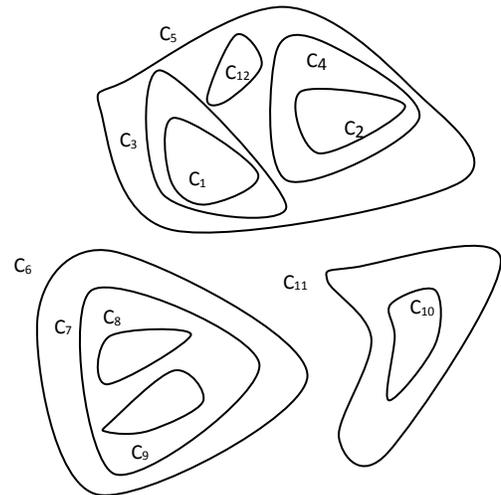


Fig.1 Contours in composition structure of tree type

Relational position aspect between two contours it defined, used the function position relation :

$$RELPOZ(C_1, C_2) \rightarrow \{INTERIOR, EXTERIOR, INTERSECTION, IDENTICAL\}$$

For the contours structure from Fig.1 , it obtain $N = n^2, n = 12$ relations which are evidenced through the table $M_{12,12}$ (Fig.3) which it note by

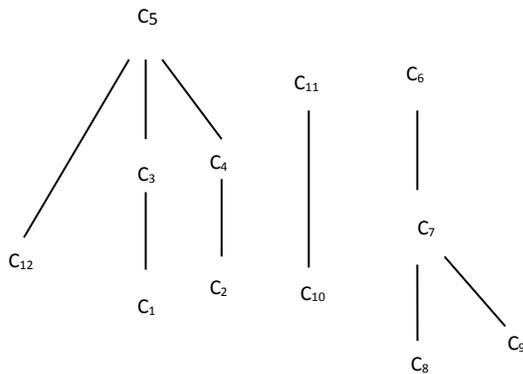


Fig.2 Graphic representation of a structure from Fig.1

1-INTERIOR relation, Blank-EXTERIOR relation, and with 2- SURROUND relation. It make the observation that surround relation it obtain by tree rule:

$$X \text{ INTERIOR } Y \text{ IF- } Y \text{ SURROUND } X \quad (2)$$

In the Fig.2 it observed that in a tree structure it can evidence : BRANCH relation and BRANCHING relation. Defining of relations in a tree structure [2] it make by predicative formulas (3) , with observation that from position relations mass , possible between two contours , it considers only INTERIOR relation:

$$R1: X \text{ INTERIOR } Y \vdash Y(X) \quad (3)$$

$$R2: Y(A), A(Z) \vdash Y(A(Z))$$

$$R3: Y(A), Y(B), Y(C) \dots Y(Z) \vdash Y(A, B, C, \dots Z)$$

Table 1

	C ₁	C ₂	C ₃	C ₄	C ₅	C ₆	C ₇	C ₈	C ₉	C ₁₀	C ₁₁	C ₁₂	
C ₁	x		1		1								
C ₂		x		1	1								
C ₃	2		x		1								
C ₄		2		x	1								
C ₅	2	2	2	2	x							2	
C ₆						x	2	2	2				
C ₇						1	x	2	2				
C ₈						1	1	x					
C ₉						1	1			x			
C ₁₀											x	1	
C ₁₁										2		x	
C ₁₂					1								x

Fig.3 Relation Table M_{12,12}

Rule R1 from the relation (3) ,define ARROW notion considered as arc having as domain the knot Y and knot X as codomain.

Rule R2 from the relation (3), it is an interference rule what can be extended so:

$$Y(A), A(B), B(C), \dots X(Y), Y(Z) \vdash Y(A(B(C \dots X(Y(Z)), \dots Z))) \quad (4)$$

defining the BRANCH relation as the way from the knot Y to knot Z in a tree. The number of arrows from knot Y to knot Z it names the length way and it note with $l(Y,Z)=k-l$ where k represents the number of knots belong at the some way[3].

Rule R3 from the relation (3) , which determine BRANCHING rule lead at the tree definition $a=Y(A,B,C\dots Z)$ where Y is the root and A,B,C...Z are under tree.

Algorithm proposed by Dora Florea in this paper, which leads at the representation of a composition structure with add of a structure list L (1) , having as the initial date the position relation of type INTERIOR which are between atomic elements existent in the Relation Table M_{12,12} (Fig.3) , it following:

Step1. Determination of final secvnt Z_i , eliminating from the symbols mass M_c , the defined elements as the fields of possible arrows in the tree $S = \{z_i | i = 1 \dots f\}$

Step2. Determination the ways from the final secvnt at the initial secvnt, which suppose:

2.1 To find out arrows which contain final secvnt through application rule R1

2.2 Determination of length ways $l_i(X_i, Z_i), i=1 \dots f = q$ where q is the number of arrows what contains the final secvnt Z_i

2.3 Considering $\theta^i = \{x_1^i, x_2^i, \dots, x_p^i\}$ symbol mass what define arrows having domains with the same codomains Z_i , it establish all arows of which domains and codomains belong mass $\theta^i \cup \{Z_i\}$. From the observation that the initial secvnt of way , represents the domain with the most codomains and in sequence if the subtract the level in tree , the number of codomains it subtract with 1, so last but one secvnt represents domain of a single codomain, it establish the way from initial secvnt $X_j^i, j \in \{1 \dots p\}$ at the final secvnt Z_i so:

2.3.1 It define the function $f(f_j^i) = m, m \geq 1$ where m is arrows number what have the same field $X_j^i \in \theta^i$

2.3.2 Sequence knots from tree in the way from X_j^i to final kot Z_i is dictate of function f , of which value decrease from initial secvent at final secvent.

So if $f(X_k^i) = m, f(X_z^i) = m - 1, f(X_w^i) = 1$ where $(k, z, ..w) \in [1, p]$, the way d_i in the tree is succession of secvents $X_k^i(X_z^i(\dots(X_w^i(Z_i))\dots)) = d_i$ obtains by application of interference rule R_2 .

Step3. Determination description list of tree structure L (1):

From Step2,results relations of type $X_i(L_1), X_i(L_2), \dots, X_i(L_j)$ what describe existing ways from initial secvent X_i at final secvents.

Used the interference rule R_3 (3) what define relation of BRANCHING, results:

$$X_i(L_1), X_i(L_2), \dots, X_i(L_j) \vdash X_i(L_1, L_2, \dots, L_j). \quad (5)$$

At its order each element of lists $L_{i,i=1..j}$ may represents a list $L_k = X_j(L_{kj}), k \in [1, j]$ at which it apply the interference rule R_3 (3) if is the case.

EXEMPLIFICAION OF ALGORITHM APPLICATION

Algorithm stages traversing for example from Fig.1 exist in the Table 2 ,Fig.4, having as input dates (6) , for a particular case, relations between eleven contours, as following application of interference rule R_1 (3) ,starting from representation of the structure presented in the fig.2:

$$C_3(C_1), C_5(C_1), C_5(C_3), C_5(C_4), C_5(C_2), C_4(C_2), C_5(C_{12}), C_6(C_7), C_6(C_8), C_7(C_8), C_6(C_9), C_7(C_9), C_{11}(C_{10}), \quad (6)$$

Table 2

Step 1 Determination final secvents : $Z_{i,i=1..6} = \{C_1, C_2, C_8, C_9, C_{10}, C_{12}\}$

Step 2. 2.1Determination arrows from (6) what contains final secvents $Z_{i,i=1..6}$

$$\begin{matrix} Z_1=C_1 & Z_2=C_2 & Z_3=C_8 & Z_4=C_9 \\ Z_5=C_{10} & Z_6=C_{12} & & \end{matrix}$$

$$\begin{matrix} C_3(C_1) & C_5(C_2) & C_6(C_8) & C_7(C_9) & C_{11}(C_{10}) & C_5(C_{12}) \\ C_5(C_1) & C_4(C_2) & C_7(C_8) & C_6(C_9) & & \end{matrix}$$

2.2 Establish length ways $l_i(x_i, z_i)$

$$\begin{matrix} l_1=2 & & l_2=2 & & l_3=2 & & \\ & l_4=2 & & l_5=1 & & l_6=1 & \end{matrix}$$

2.3 Determination ways $d_{i,i=1..6}$ from initial secvents at final secvents $Z_{i,i=1..6}$

$$\begin{matrix} Z_1=C_1 & \text{Arrows} & \in \{\theta^1 \cup \{Z_1\}, \text{where} & \theta^1 = \{C_3, C_5\}, \\ C_3(C_1) & C_3(C_1) & C_5(C_1) & f(C_5) = 2 \\ C_5(C_1) & & C_5(C_3) & f(C_3) = 1 \\ C_5(C_3) & & & \\ & & & d_1 = C_5(C_3(C_1)) \end{matrix}$$

$$\begin{matrix} Z_2=C_2 & \text{Arrows} & \in \{\theta^2 \cup \{Z_2\}, \text{where} & \theta^2 = \{C_4, C_5\}, \\ C_4(C_2) & C_4(C_2) & C_5(C_2) & f(C_5) = 2 \\ C_5(C_2) & & C_5(C_4) & f(C_4) = 1 \\ & & & d_2 = C_5(C_4(C_2)) \end{matrix}$$

$$\begin{matrix} Z_3=C_8 & \text{Arrows} & \in \{\theta^3 \cup \{Z_3\}, \text{where} & \theta^3 = \{C_6, C_7\}, \\ C_7(C_8) & C_7(C_8) & C_6(C_8) & f(C_6) = 2 \\ C_6(C_8) & & C_6(C_7) & f(C_7) = 1 \\ C_6(C_7) & & & \\ & & & d_3 = C_6(C_7(C_8)) \end{matrix}$$

$$\begin{matrix} Z_4=C_9 & \text{Arrows} & \in \{\theta^4 \cup \{Z_4\}, \text{where} & \theta^4 = \{C_6, C_7\}, \\ C_7(C_9) & C_7(C_9) & C_6(C_9) & f(C_6) = 2 \\ C_6(C_9) & & C_6(C_7) & f(C_7) = 1 \\ C_6(C_7) & & & \\ & & & d_4 = C_6(C_7(C_9)) \end{matrix}$$

$$\text{Arrows} \in \{\theta^5 \cup \{Z_5\}, \text{where} \theta^5 = \{C_5\}, Z_5=C_{12}$$

$$C_5(C_{12})$$

$$d_5 = C_5(C_{12})$$

Arrows $\in \{\theta^6 \cup \{Z_6\}, \text{where } \theta^6 = \{C_{11}\}, Z_6 = C_{10}$

$$C_{11}(C_{10})$$

$$d_6 = C_{11}(C_{10})$$

Step 3 Determination describe lists of structure L :

$$L_1: C_5(C_3(C_1)), C_5(C_4(C_2)), C_5(C_{12}) \vdash C_5(C_3(C_1), C_4(C_2), C_{12})$$

$$L_2: C_6(C_7(C_8)), C_6(C_7(C_9)) \vdash C_6(C_7(C_8), C_7(C_9)) \vdash C_6(C_7(C_8, C_9))$$

$$L_3: C_{11}(C_{10})$$

$$L = (L_1, L_2, L_3) = (C_5(C_3(C_1), C_4(C_2), C_{12}), C_6(C_7(C_8, C_9)), C_{11}(C_{10}))$$

Fig.4 Algorithm for the particular case from Fig.1

CONCLUSION

Original method of Dora Florea presents in this paper through which it allow determination coplanar contours hierarchy of a mass through an tree structure expressed under structure list form is very simple. The algorithm was checked up by a program wrote in Visual Basic language. It appreciate that it necessary small input dates, that being position relations of the type *INTERIOR*, identificate between the mass contours.

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