

INTERNATIONAL JOURNAL OF ENGINEERING SCIENCES & RESEARCH TECHNOLOGY
HIERARCHY OF PLANE CONTOURS THROUGH TREES STRUCTURES WITH THE STRUCTURE LIST
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ABSTRACT

Paper presents an original method proposed by Dora Florea for hierarchy of the plane contours in trees structures, express through a structure liste, starting from the knowledge the position relation between two contours.

KEYWORDS: Plane contour, tree structure, position relation, hierarchy

INTRODUCTION

A matricial representation of the trees was proposed by T.Rus [1] and so it know the reprezentation of a contours tree structure by structure list .

Requiring position relation aspect between two by two contours , belong of a contours collection defined as atomic objects expresses with the matricial representation , in this paper Dora Florea propose an original method to obtain a composition structure of the tree or forest composed from atomic objects which are contours express with add the structure list.

THEORETICAL CONSIDERATION

Beeing gived the contours collection $M_c = \{C_i | i = 1..n\}$ closed and coplain, contours may be considered as the atomic objects of a complex structure of which composition may be describe by a tree or forest atomic objects. In Fig.1 it evidences an composition tree of a forest type composed from 3 disjunct trees and which it may be graphic presents as in Fig.2.

Contours structure from Fig.1 may be represents by a structure list:

$$\begin{aligned} L = & (C_5(C_3(C_1), C_4(C_2), C_{12}, C_6(C_7(C_8, C_9)), C_{11} \\ & (C_{10})) \end{aligned} \quad (1)$$

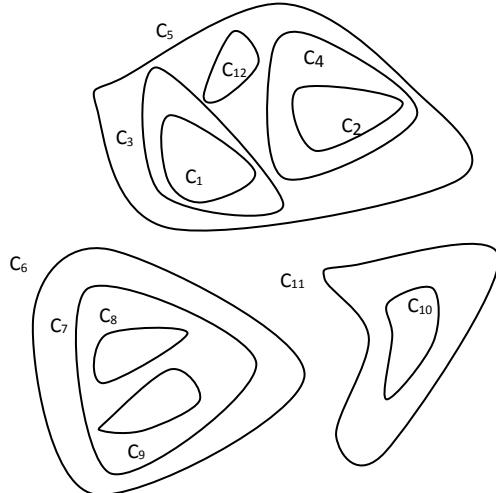


Fig.1 Contours in composition structure of tree type

Relational position aspect between two contours it defined, used the function position relation :

$$\begin{aligned} RELPOZ(C_1, C_2) \\ \rightarrow & \{INTERIOR, EXTERIOR, INTERSECTION, \\ & IDENTICAL\} \end{aligned}$$

For the contours structure from Fig.1 , it obtain $N = n^2, n = 12$ relations which are evidenced through the table $M_{12,12}$ (Fig.3) which it note by

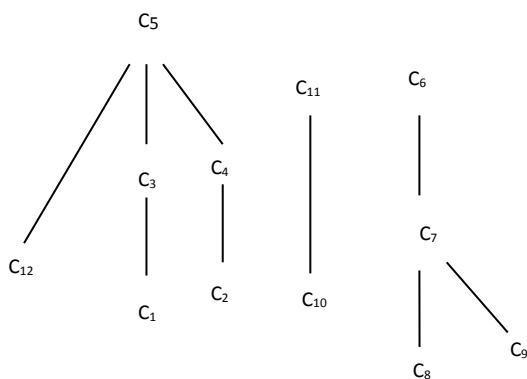


Fig.2 Graphic representation of a structure from Fig.1

I-INTERIOR relation, Blank-*EXTERIOR* relation, and with *2- SURROUND* relation.

It make the observation that surround relation it obtain by tree rule:

$$X \text{ INTERIOR } Y \Vdash Y \text{ SURROUND } X \quad (2)$$

In the Fig.2 it observed that in a tree structure it can evidence : *BRANCH* relation and *BRANCHING* relation.

Defining of relations in a tree structure [2] it make by predicative formulas (3) , with observation that from position relations mass , possible between two contours , it considers only *INTERIOR* relation:

$$R1: X \text{ INTERIOR } Y \vdash Y(X) \quad (3)$$

$$R2: Y(A), A(Z) \vdash Y(A(Z))$$

$$R3: Y(A), Y(B), Y(C) \dots Y(Z) \vdash Y(A, B, C, \dots, Z)$$

Table 1

	C ₁	C ₂	C ₃	C ₄	C ₅	C ₆	C ₇	C ₈	C ₉	C ₁₀	C ₁₁	C ₁₂
C ₁	x		1		1							
C ₂		x		1	1							
C ₃	2		x		1							
C ₄		2		x	1							
C ₅	2	2	2	2	x							2
C ₆						x	2	2	2			
C ₇						1	x	2	2			
C ₈						1	1	x				
C ₉						1	1		x			
C ₁₀									x	1		
C ₁₁									2	x		
C ₁₂					1						x	

Fig.3 Relation Table M_{12,12}

Rule R1 from the relation (3) ,define *ARROW* notion considered as arc having as domain the knot Y and knot X as codomain.

Rule R2 from the relation (3), it is an interference rule what can be extended so:

$$Y(A), A(B), B(C), \dots X(Y), Y(Z) \vdash Y(A(B(C \dots X(Y(Z)), \dots Z)) \quad (4)$$

defining the *BRANCH* relation as the way from the knot Y to knot Z in a tree.

The number of arrows from knot Y to knot Z it names the length way and it note with $l(Y,Z)=k-1$ where k represents the number of knots belong at the same way[3].

Rule R3 from the relation (3) , which determine *BRANCHNG* rule lead at the tree definition $a=Y(A,B,C\dots Z)$ where Y is the root and A,B,C...Z are under tree.

Algorithm proposed by Dora Florea in this paper,which leads at the representation of a composition structure with add of a structure list L (1) , having as the initial date the position relation of type *INTERIOR* which are between atomic elements existent in the Relation Table M_{12,12} (Fig.3) , it following:

Step1. Determination of final secent Z_i , eliminating from the symbols mass M_c , the defined elements as the fields of possible arrows in the tree $S = \{z_i | i = 1 \dots f\}$

Step2. Determination the ways from the final secent at the initial secent, which suppose:

2.1 To find out arrows which contain final secent through application rule *R1*

2.2 Determination of length ways $l_i(X_i, Z_i), i=1 \dots f = q$ where q is the number of arrows what contains the final secent Z_i

2.3 Considering $\theta^i = \{x_1^i, x_2^i, \dots x_p^i\}$ symbol mass what define arrows having domains with the same codomains Z_i , it establish all arrows of which domains and codomains belong mass $\theta^i \cup \{Z_i\}$. From the observation that the initial secent of way , represents the domain with the most codomains and in sequence if the subtract the level in tree , the number of codomains it subtract with 1, so last but one secvnt represents domain of a single codomain, it establish the way from initial secent $X_j^i, j \in \{1 \dots p\}$ at the final secent Z_i so:

2.3.1 It define the function $f(f_j^i) = m, m \geq 1$ where m is arrows number what have the same field $X_j^i \in \theta^i$

2.3.2 Sequence knots from tree in the way from X_j^i to final knot Z_i is dictate of function f , of which value descrease from initial secent at final secent.

So if $f(X_k^i) = m, f(X_z^i) = m - 1, f(X_w^i) = 1$ where $(k, z, \dots w) \in [1, p]$, the way d_i in the tree is succession of secents $X_k^i(X_z^i(\dots X_w^i(Z_i))\dots) = d_i$ obtains by application of interference rule R2.

Step3. Determination description list of tree structure L (1):

From Step2, results relations of type $X_i(L_1), X_i(L_2), \dots X_i(L_j)$ what describe existing ways from initial secent X_i at final secents.

Used the interference rule R3 (3) what define relation of BRANCHING, results:

$$X_i(L_1), X_i(L_2), \dots X_i(L_j) \vdash X_i(L_1, L_2, \dots L_j). \quad (5)$$

At its order each element of lists $L_{i,i=1\dots j}$ may represents a list $L_k = X_j(L_{kj}), k \in [1, j]$ at which it apply the interference rule R3 (3) if is the case.

EXEMPLIFICAION OF ALGORITHM APPLICATION

Algorithm stages traversing for example from Fig.1 exist in the Table 2 ,Fig.4, having as input dates (6) , for a particular case, relations between eleven contours, as following application of interference rule R1 (3) ,starting from representation of the structure presented in the fig.2:

$$\begin{aligned} C_3(C_1), C_5(C_1), C_5(C_3), C_5(C_4), C_5(C_2), C_4(C_2), C_5(C_{12}), C_6(C_7), \\ C_6(C_8), C_7(C_8), C_6(C_9), C_7(C_9), C_{11}(C_{10}), \end{aligned} \quad (6)$$

Table 2

Step 1 Determination final secents : $Z_{i,i=1..6} = \{C_1, C_2, C_8, C_9, C_{10}, C_{12}\}$

Step 2. 2.1Determination arrows from (6) what contains final secents $Z_{i,i=1..6}$

$$\begin{aligned} Z_1=C_1 & \quad Z_2=C_2 & \quad Z_3=C_8 & \quad Z_4=C_9 \\ Z_5=C_{10} & \quad Z_6=C_{12} & & \end{aligned}$$

$$\begin{aligned} C_3(C_1) & \quad C_5(C_2) & \quad C_6(C_8) & \quad C_7(C_9) & \quad C_{11}(C_{10}) & \quad C_5(C_{12}) \\ C_5(C_1) & \quad C_4(C_2) & \quad C_7(C_8) & \quad C_6(C_9) & & \end{aligned}$$

2.2 Establish length ways $l_i(x_i, z_i)$

$$\begin{array}{lll} l_1=2 & l_2=2 & l_3=2 \\ l_4=2 & l_5=1 & l_6=1 \end{array}$$

2.3 Determination ways $d_{i,i=1..6}$ from initial secents at final secents $Z_{i,i=1..6}$

$$\text{Arrows } \in \{\theta^1 \cup \{Z_1\}\}, \text{where } \theta^1 = \{C_3, C_5\}, \\ Z_1=C_1$$

$$\begin{array}{lll} C_3(C_1) & C_3(C_1) & C_5(C_1) \\ C_5(C_1) & & C_5(C_3) \\ C_5(C_3) & & \end{array} \quad \begin{array}{ll} f(C_5) = 2 \\ f(C_3) = 1 \end{array}$$

$$d_1 = C_5(C_3(C_1))$$

$$\text{Arrows } \in \{\theta^2 \cup \{Z_2\}\}, \text{where } \theta^2 = \{C_4, C_5\}, \\ Z_2=C_2$$

$$\begin{array}{lll} C_4(C_2) & C_4(C_2) & C_5(C_2) \\ C_5(C_2) & & C_5(C_4) \end{array} \quad \begin{array}{ll} f(C_5) = 2 \\ f(C_4) = 1 \end{array}$$

$$d_2 = C_5(C_4(C_2))$$

$$\text{Arrows } \in \{\theta^3 \cup \{Z_3\}\}, \text{where } \theta^3 = \{C_6, C_7\}, \\ Z_3=C_8$$

$$\begin{array}{lll} C_7(C_8) & C_7(C_8) & C_6(C_8) \\ C_6(C_8) & & C_6(C_7) \\ C_6(C_7) & & \end{array} \quad \begin{array}{ll} f(C_6) = 2 \\ f(C_7) = 1 \end{array}$$

$$d_3 = C_6(C_7(C_8))$$

$$\text{Arrows } \in \{\theta^4 \cup \{Z_4\}\}, \text{where } \theta^4 = \{C_6, C_7\}, \\ Z_4=C_9$$

$$\begin{array}{lll} C_7(C_9) & C_7(C_9) & C_6(C_9) \\ C_6(C_9) & & C_6(C_7) \\ C_6(C_7) & & \end{array} \quad \begin{array}{ll} f(C_6) = 2 \\ f(C_7) = 1 \end{array}$$

$$d_4 = C_6(C_7(C_9))$$

$$\text{Arrows } \in \{\theta^5 \cup \{Z_5\}\}, \text{where } \theta^5 = \{C_5\}, Z_5=C_{12}$$

$C_5(C_{12})$ $d_5 = C_5(C_{12})$ Arrows $\in \{\theta^6 \cup \{Z_6\}\}$, where $\theta^6 = \{C_{11}\}$, $Z_6 = C_{10}$ $C_{11}(C_{10})$ $d_6 = C_{11}(C_{10})$

Step 3 Determination describe lists of structure L :

 $L_1: C_5(C_3(C_1)), C_5(C_4(C_2)), C_5(C_{12}) \vdash C_5(C_3(C_1), C_4(C_2), C_{12})$
 $L_2: C_6(C_7(C_8)), C_6(C_7(C_9)) \vdash C_6(C_7(C_8), C_7(C_9)) \vdash C_6(C_7(C_8, C_9))$
 $L_3: C_{11}(C_{10})$
 $L = (L_1, L_2, L_3) = (C_5(C_3(C_1), C_4(C_2), C_{12}), C_6(C_7(C_8, C_9)), C_{11}(C_{10}))$
Fig.4 Algorithm for the particular case from Fig.1

CONCLUSION

Original method of Dora Florea presents in this paper through which it allow determination coplanar contours hierarchy of a mass through an tree structure expressed under structure list form is very simple. The algorithm was check up by a program wrote in Visual Basic language. It appreciate that it necessary small input dates ,that beeing position relations of the type *INTERIOR* , identificate between the mass contors.

ACKNOWLEDGEMENTS

I take this opportunity to express my gratitude to the people who have been instrumental in the successful completion of this work.

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